

# **“Eccentricity pumping of exoplanets by tidal effect”**

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# Tidal effects



# moderate close-in planets

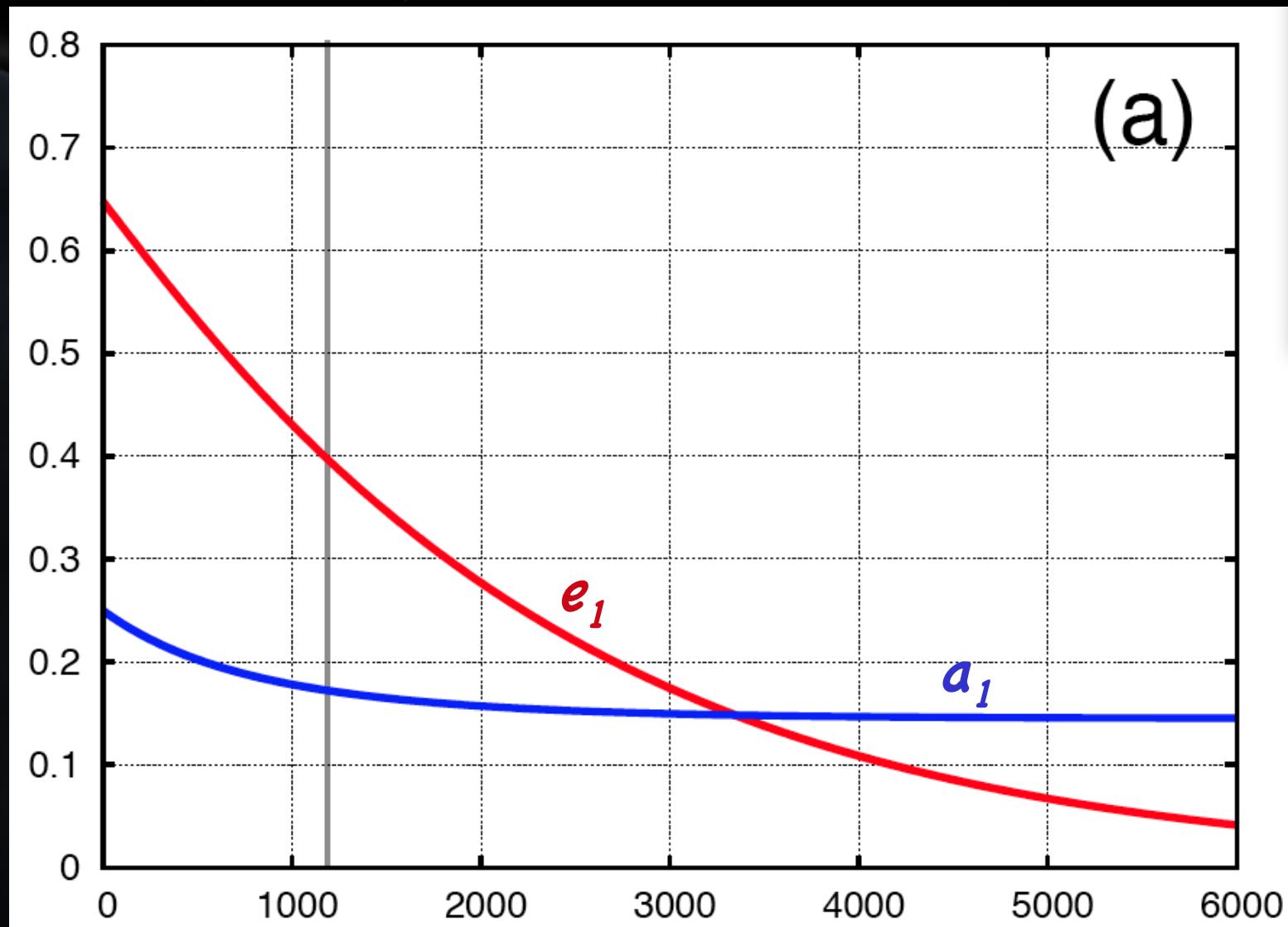
**Table 1**

Single Planetary Systems with  $0.1 < a_1 < 0.3$  and  $e_1 > 0.3$

Star (Name)	$a_1$ (AU)	$e_1$	$m_1$ ( $M_J$ )	$m_0$ ( $M_\odot$ )	Age (Gyr)	$\tau$ (Gyr)
HD 108147	0.102	0.53	0.26	1.19	2.0	0.01
CoRoT-10	0.105	0.53	2.75	0.89	3.0	0.24
HD 33283	0.145	0.48	0.33	1.24	3.2	0.34
HD 17156	0.163	0.68	3.19	1.28	3.4	0.44
HIP 57050	0.164	0.31	0.30	0.34	...	39.4
HD 117618	0.176	0.42	0.18	1.05	3.9	2.06
HD 45652	0.228	0.38	0.47	0.83	...	93.3
HD 90156	0.250	0.31	0.06	0.84	4.4	35.8
HD 37605	0.260	0.74	2.84	0.80	10.7	10.6
HD 3651	0.284	0.63	0.20	0.79	5.1	15.5

# eccentricity damping

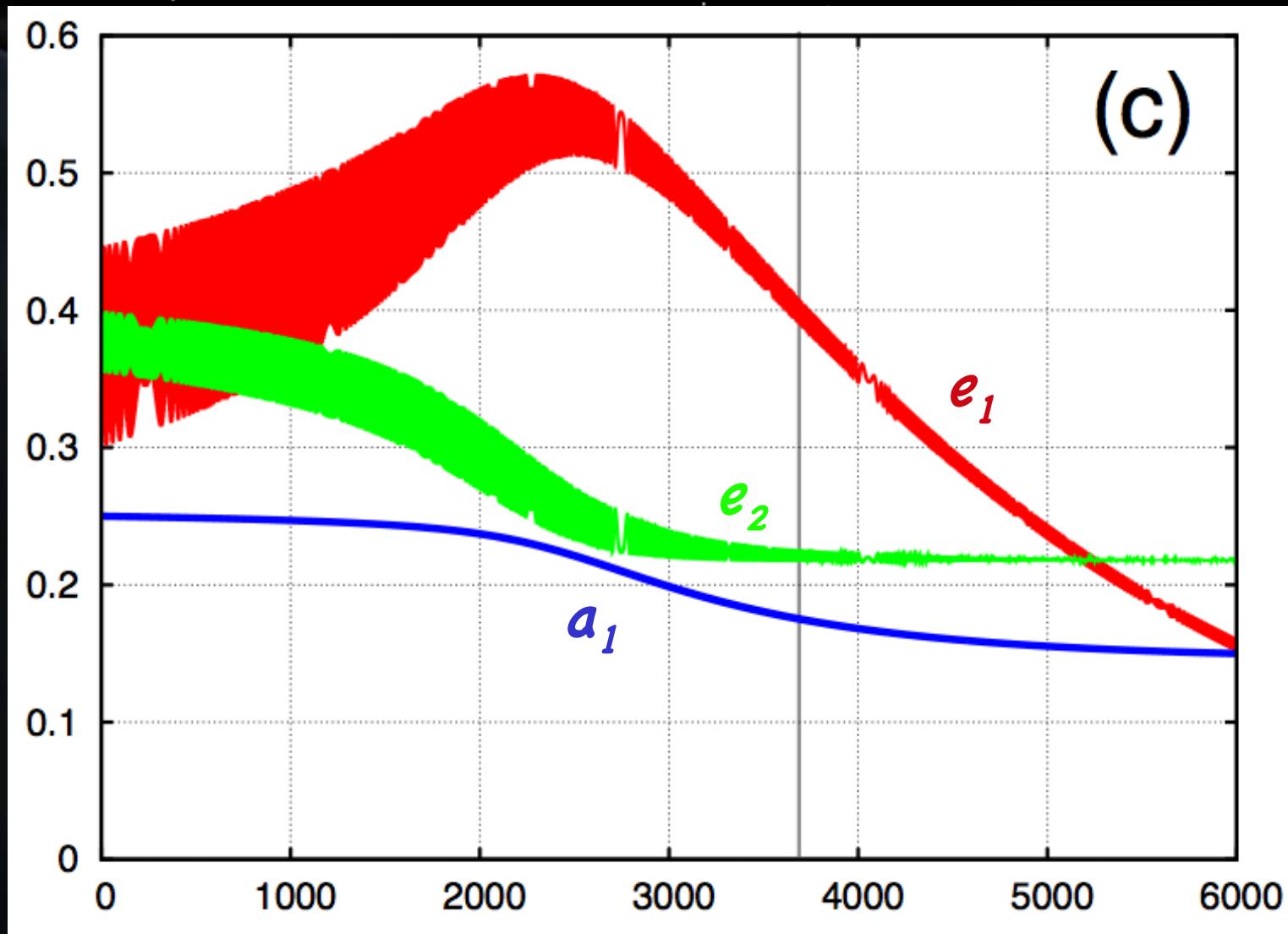
HD 117618 b



Correia, Boué & Laskar, *ApJ Lett* (2012)

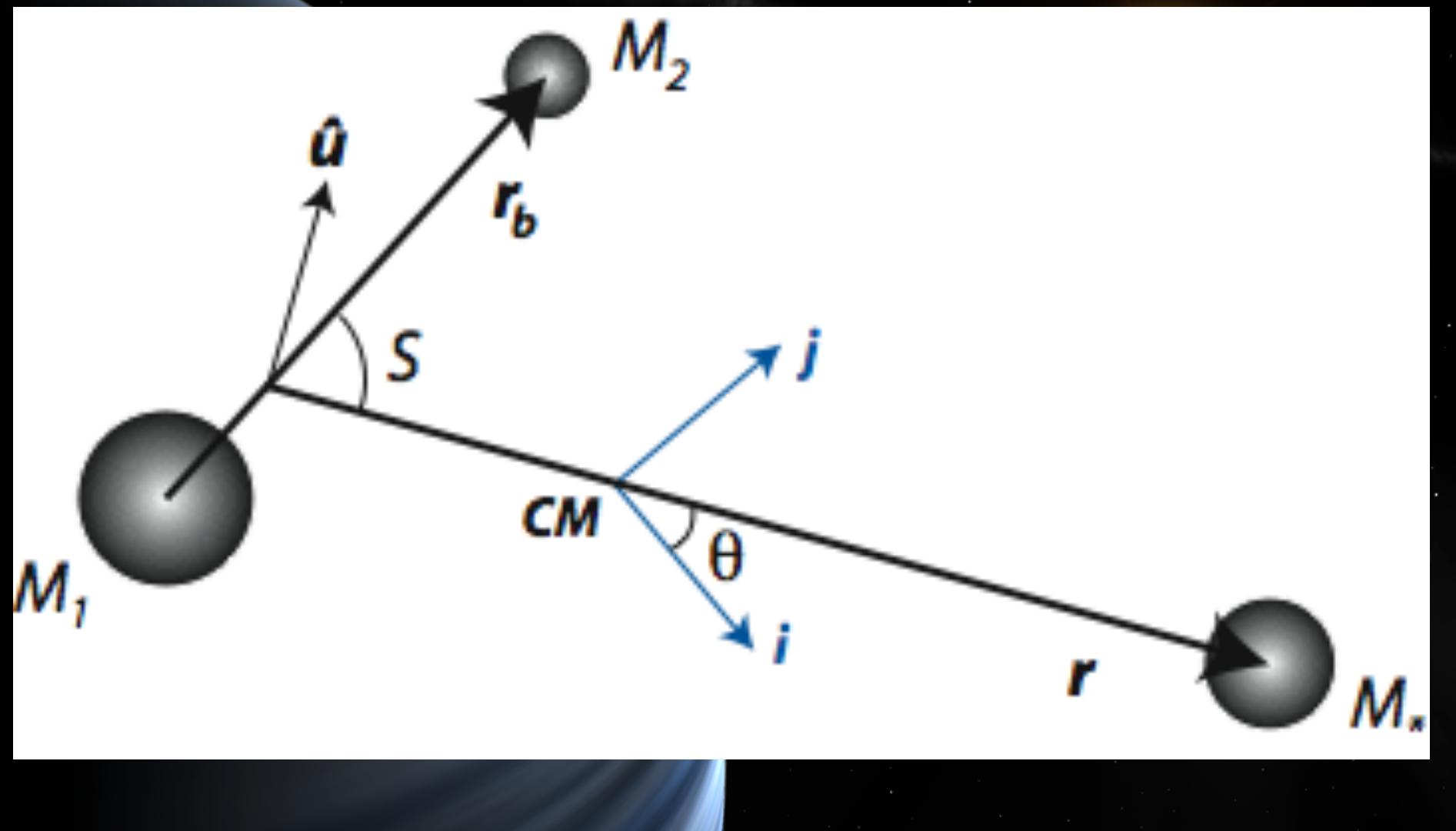
# eccentricity pumping

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Correia, Boué & Laskar, *ApJ Lett* (2012)

# planar 3-body problem (not restricted + octupolar approx.)



# Conservative energy

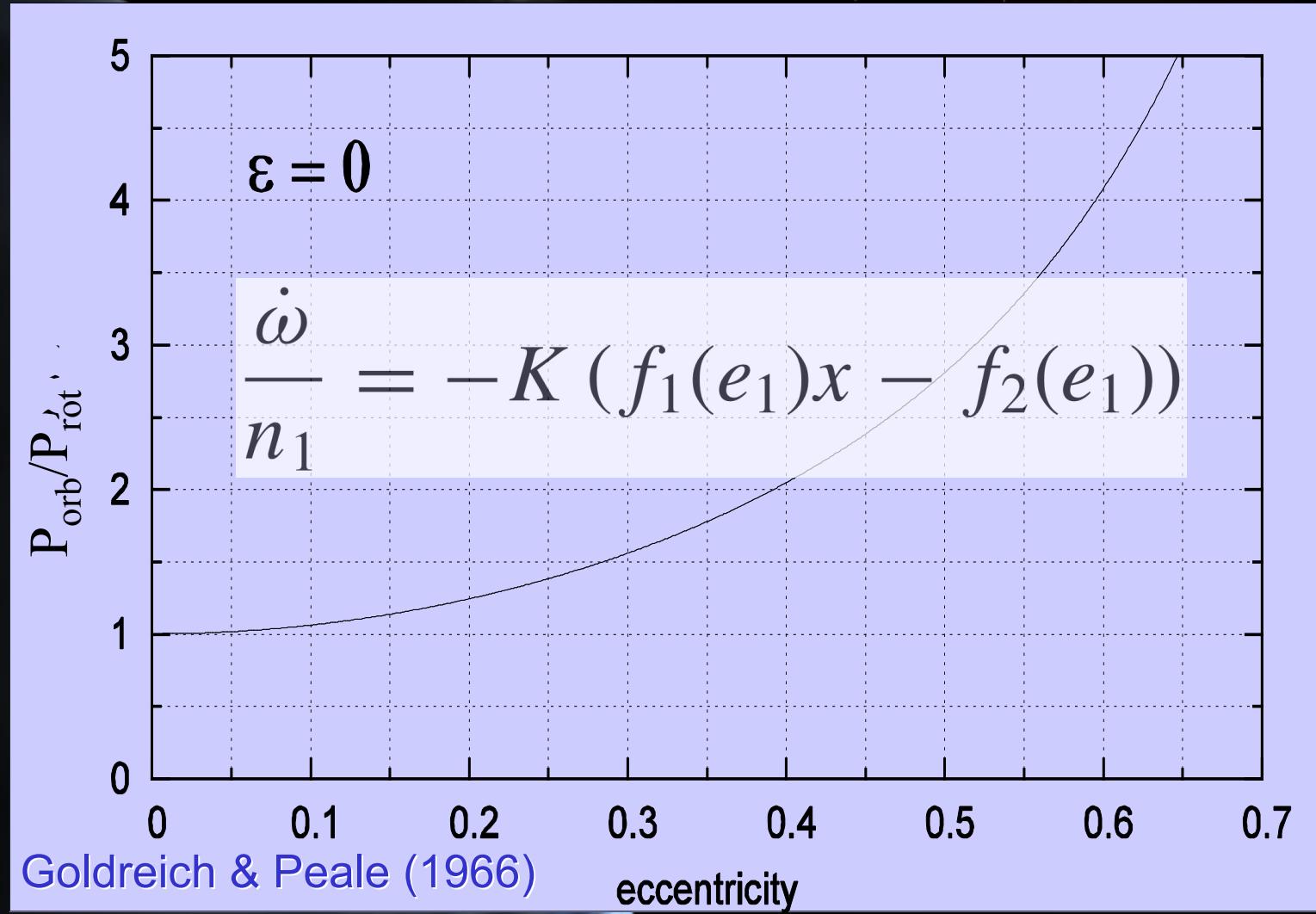
## relativity + spin + octupolar approx.

$$U = -C_0 \frac{(1 - \omega^2)^{-1/2}}{r} - C_1 \frac{(1 - \omega^2)^{-3/2}}{r^3} \omega^2 R^3 - C_2 J_2 = k_2 \frac{\omega^2 R^3}{3Gm_1} \cos \varpi,$$

$$C_0 = \frac{3\beta_1 G^2 (m_0 + m_1)^2}{a_1^2 c^2}, \quad C_1 = \frac{Gm_0 m_1 J_2 R^2}{2a_1^3},$$

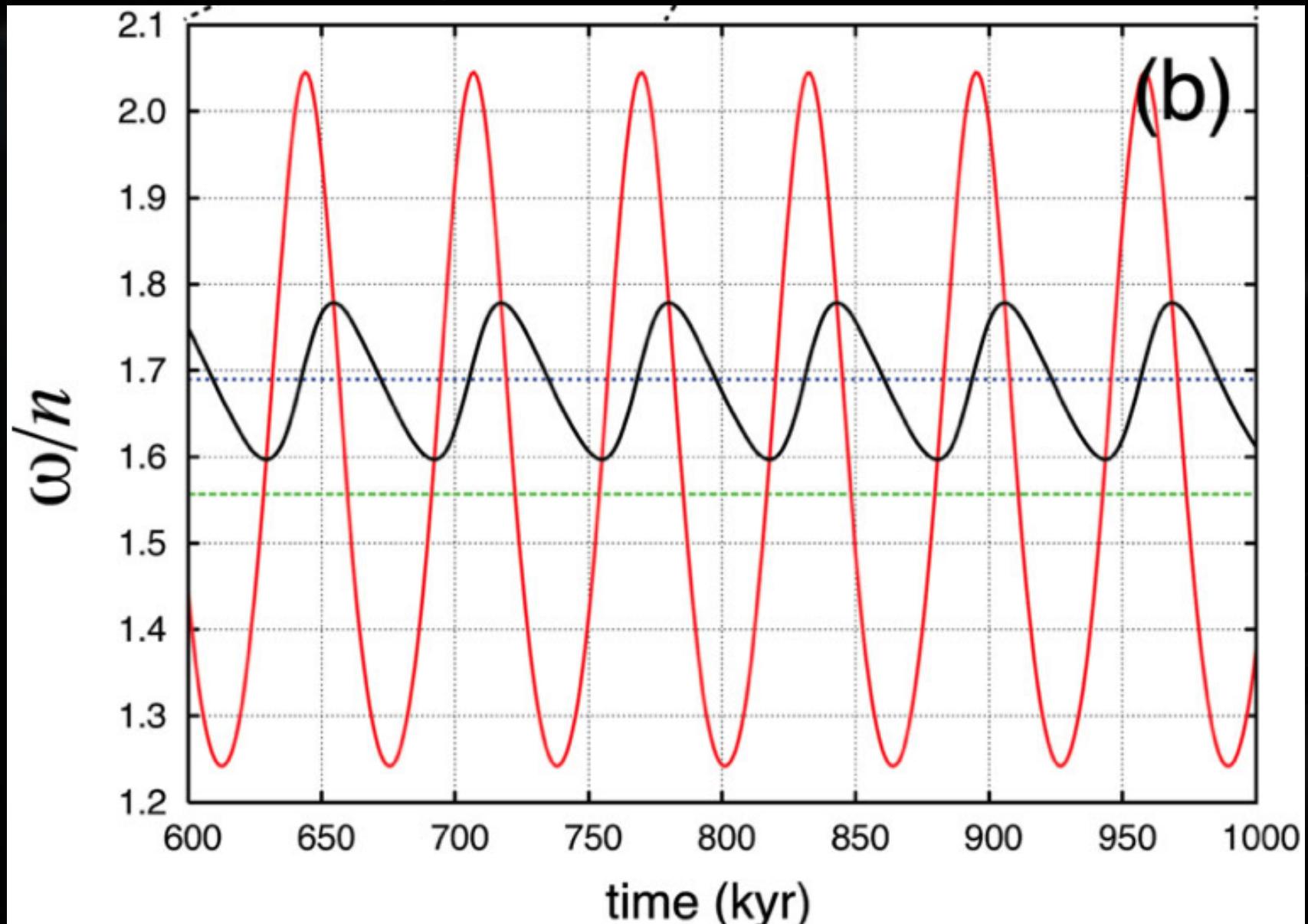
$$C_2 = \frac{G\beta_1 m_2 a_1^2}{4a_2^3}, \quad C_3 = \frac{15G\beta_1 m_2 a_1^3}{16a_2^4} \frac{(m_0 - m_1)}{m_0 + m_1},$$

# Intermediate evolution:

$$\omega_{\text{eq}} / n = f_2/f_1(e)$$


Jupiter-size planets

# Rotation tidal wobble



# Equations of motion

$$\dot{e}_1 = -\nu_{31} \frac{e_2 (1 + 3/4 e_1^2) \sqrt{1 - e_1^2}}{(1 - e_2^2)^{5/2}} \sin \varpi$$

$$\begin{aligned} \dot{\varpi} = & \frac{\nu_0}{(1 - e_1^2)} + \frac{\nu_1 x^2}{(1 - e_1^2)^2} \\ & + \nu_{21} \frac{\sqrt{1 - e_1^2}}{(1 - e_2^2)^{3/2}} - \nu_{22} \frac{(1 + \frac{3}{2} e_1^2)}{(1 - e_2^2)^2} \end{aligned}$$

$$\frac{\dot{\omega}}{n_1} = -K (f_1(e_1)x - f_2(e_1))$$

# linearized system

$$\delta \dot{e}_1 = -A \sin \varpi,$$

$$\boxed{\delta e_1 = \Delta e \cos(gt + \varpi_0)}$$

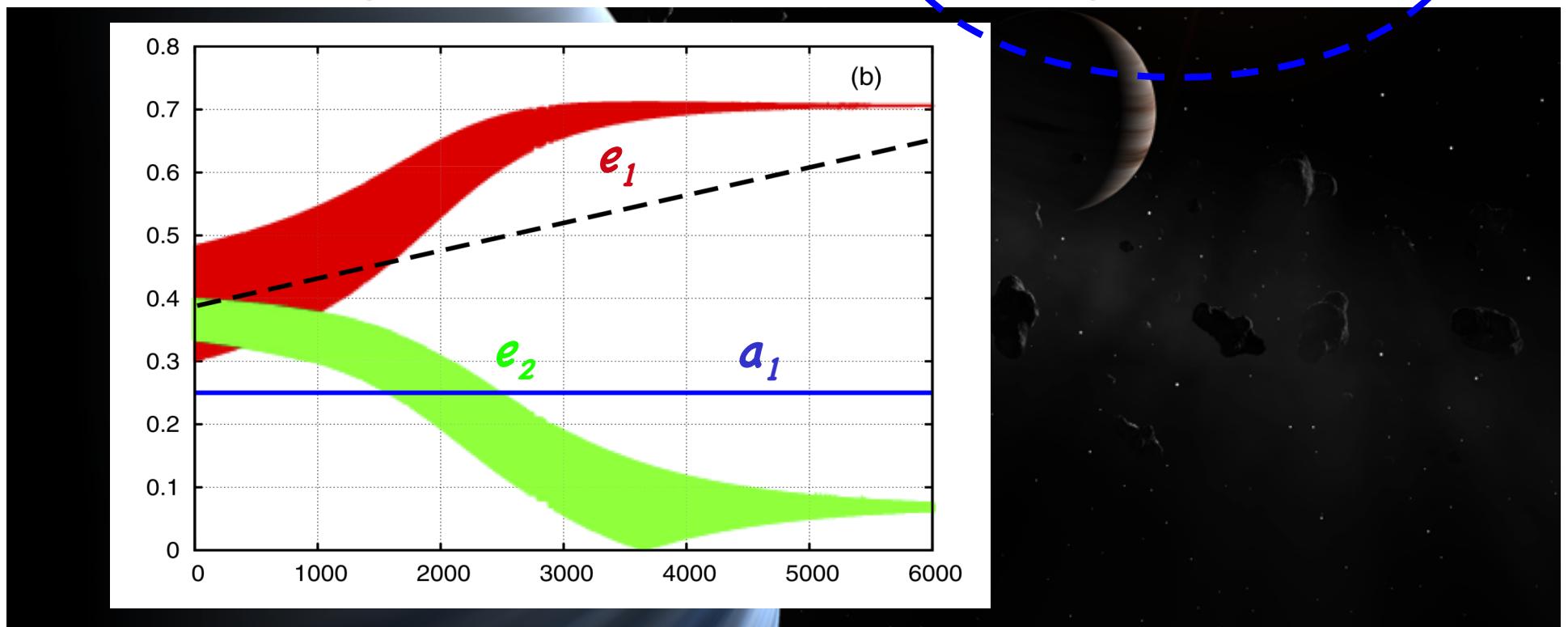
$$\dot{\varpi} = g$$

$$\boxed{\delta x = \Delta x \cos(gt + \varpi_0 - \phi)}$$

$$\delta \dot{x} = -\nu_x \delta x + \nu_e \delta e_1,$$

# drift on the eccentricity

$$\begin{aligned}\delta \dot{e}_1 = & -A \sin(gt + \varpi_0) - \frac{g_x A}{2g} \Delta x \sin(2gt + 2\varpi_0 - \phi) \\ & - \frac{g_e A}{2g} \Delta e \sin(2gt + 2\varpi_0) + \frac{g_x A}{2g} \Delta x \sin \phi.\end{aligned}$$



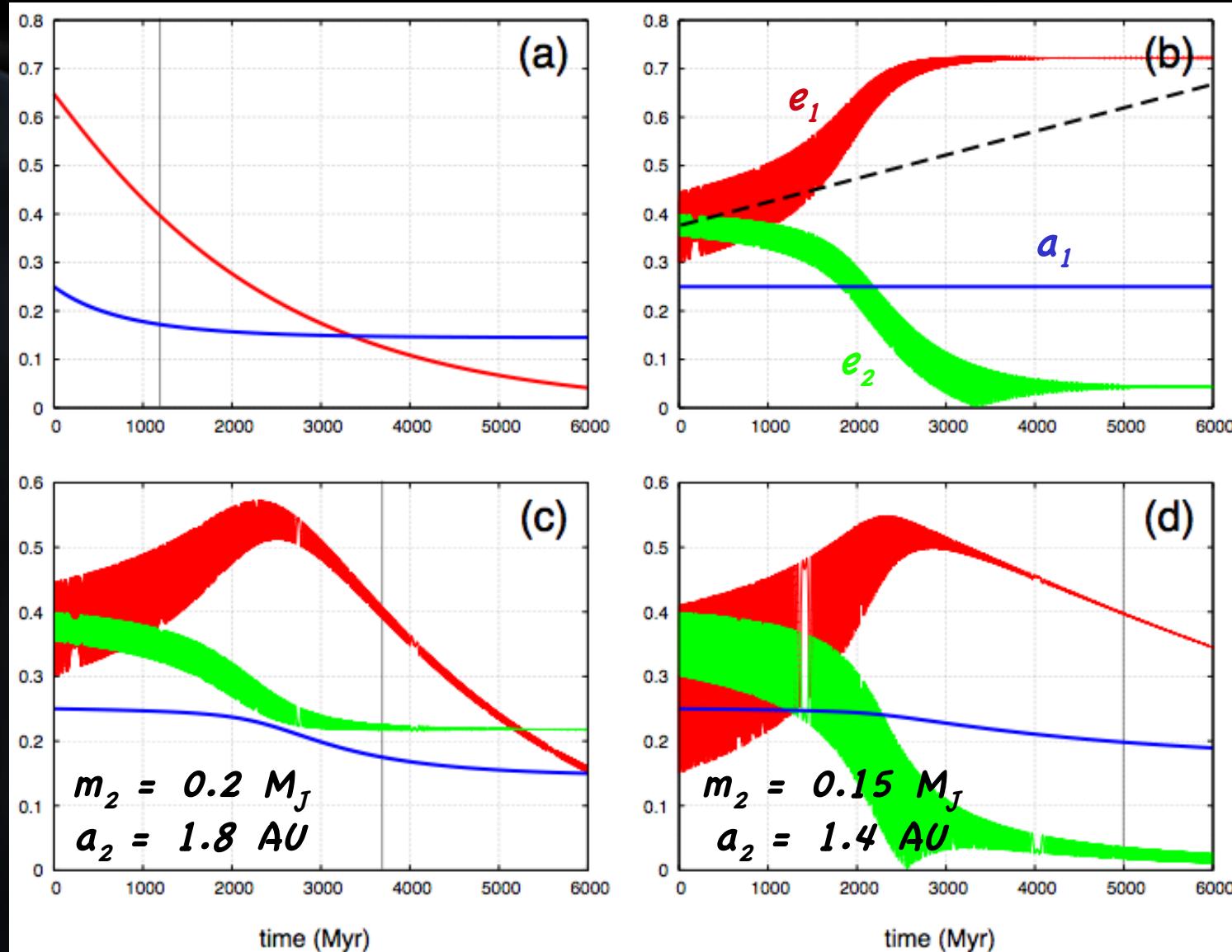
# full tidal evolution

$$\frac{\dot{a}_1}{a_1} = -7K' f_6(e_1) e_1^2,$$

$$\dot{e}_1 = -\frac{7}{2} K' f_6(e_1) \left(1 - e_1^2\right) e_1$$

HD 117618 b

# eccentricity pumping



# Conclusions

- Tidal effects are responsible for a slow secular evolution of the spins and orbits of close-in exoplanets.
- Tidal effects alone align the spin axis, synchronize the rotation and orbital periods, and damp the eccentricity of the orbit.
- Tidal effects combined with planetary perturbations may present unexpected behaviors such as the *pumping of the eccentricity*.
- The pumping effect is more effective for planets where the spin fully damped by tides, but the orbit is only slowly modified.