

Radiative processes, stellar atmospheres and winds (WS 2017)

Problem set 3

Problem 1 [5 points] *Mean intensity and Eddington/radiative flux*

- Calculate the mean intensity and the Eddington flux for an isotropic radiation field with specific intensity $I_\nu(\mu, \phi) = I_0$
- Calculate the mean intensity and the Eddington and radiative flux for an extremely anisotropic radiation field, with specific intensity $I_\nu(\mu, \phi) = I_0\delta(\mu - \mu_0)\delta(\phi - \phi_0)$ and Dirac δ -function ($-1 < \mu_0 < 1$).

Note: This situation corresponds to a monochromatic planar wave propagating into direction \vec{n}_0 (specified by angles θ_0, ϕ_0), where in vacuum $I_0 = cE_0^2/(8\pi)$, with E_0 the amplitude (absolute value) of the corresponding electric field,

$$\vec{E}(\vec{r}, t) = \vec{E}_0 \cos[2\pi(k\vec{n}_0 \cdot \vec{r} - \nu t)].$$

- Make a sketch for the situation when (i) $\mu_0 \rightarrow 1$ and (ii) $\mu_0 = 0$, and ϕ_0 has an arbitrary value $0 \leq \phi_0 < 2\pi$. Assume that the surface-normal $d\vec{S}$ is parallel to the z-axis of the coordinate-system.
- Repeat problem 1b), now with $I_\nu(\mu, \phi) = I_0\delta(\mu - \mu_0)$, where I_ν shall be independent of azimuth (i.e., plane-parallel or spherical symmetry). Compare mean intensity and Eddington flux for the two cases $\mu_0 \rightarrow 1$ and $\mu_0 = 0$, and sketch both situations again.

Problem 2 [3.5 points] *Solar constant*

The total solar radiative flux, as measured above the absorbing and reflecting terrestrial atmosphere, is given by

$$\int_0^\infty f_\nu d\nu = 1.365 \cdot 10^6 \text{ erg cm}^{-2} \text{ s}^{-1},$$

and called solar constant or solar irradiance.

- Express the solar constant in $[\text{W m}^{-2}]$.
- Calculate the effective temperature of the sun from this (and other) quantity/quantities, and the corresponding wavelengths where B_ν and B_λ obtain their maxima.
- At what distance from a 100-W light bulb (assuming the light bulb to be 100% efficient) is the radiative flux equal to the solar irradiance?

- d) Consider a model of the star ζ Puppis (the brightest O-star on the southern sky), with an effective temperature of 40,000 K, a stellar radius of $19 R_{\odot}$, and a distance of 430 pc. Determine the total radiative flux above the terrestrial atmosphere, in units of the solar constant (neglecting interstellar extinction).

Problem 3 [3.5 points] *Light in your eye*

- a) Calculate the energy of the blackbody photons in your eye. Approximate your eye by a hollow sphere of radius 1.5 cm, at a temperature of 37° C.
- b) Compare this with the energy inside your eye while looking at a 100-W light bulb that is 1 m away from you (assuming the light bulb to be 100% efficient). Adopt the area of your eye's pupil as 0.1 cm^2 .
Hint: To convert from energy per time to energy, make use of the speed of light.
- c) Why is it dark when you shut your eyes?

Have fun, and much success!